# Federated Learning over Multi-Hop Wireless Networks with In-Network Aggregation

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Abstract-Communication limitation at the edge is widely recognized as a major bottleneck for federated learning (FL). Multi-hop wireless networking provides a cost-effective solution to enhance service coverage and spectrum efficiency at the edge, which could facilitate large-scale and efficient machine learning (ML) model aggregation. However, FL over multi-hop wireless networks has rarely been investigated. In this paper, we optimize FL over wireless mesh networks by taking into account the heterogeneity in communication and computing resources at mesh routers and clients. We present a framework that each intermediate router performs in-network model aggregation before sending the data to the next hop, so as to reduce the outgoing data traffic and hence aggregate more models under limited communication resources. To accelerate model training, we formulate our optimization problem by jointly considering model aggregation, routing, and spectrum allocation. Although the problem is a non-convex mixed-integer nonlinear programming, we transform it into a mixed-integer linear programming (MILP), and develop a coarse-grained fixing procedure to solve it efficiently. Simulation results demonstrate the effectiveness of the solution approach, and the superiority of the in-network aggregation scheme over the counterpart without in-network aggregation.

Index Terms—Federated learning, multi-hop wireless network, wireless mesh network, edge computing, in-network aggregation.

#### I. INTRODUCTION

Machine learning (ML) lays the foundation for tremendous innovative applications, such as smart home, e-health, and autonomous driving. The success of ML rests on the unprecedented amount of data that can be used for model training. However, due to privacy considerations, it may be impractical to gather privacy-sensitive data, such as personal photos and videos, at a central location for training. To overcome this hurdle, federated learning (FL) has been proposed to train a global ML model across decentralized clients through model exchange without accessing clients' raw data [1]. By enabling privacy-preserving model training, FL is regarded as a key enabler for deploying ML at scale.

5G/6G cellular networks have attracted intensive interests in the last few years [2]–[4]. To unleash the potential of ML, 5G/6G and beyond are envisioned to support intelligence/computing services [5]–[7], including model inference

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and training, at the network edge. In FL, model training relies on frequent model exchange between parameter servers and a massive number of clients. Given the fact that a deep neural network generally contains millions of parameters (e.g., the popular model VGG16 contains 138 million parameters, which is 528MB in 32-bit float), the model transmissions would pose a great challenge to the wireless edge [8]. Therefore, to accelerate FL process, resource optimization for wireless networks plays a crucial role. The existing works in this field mostly focus on single-hop wireless networks, where clients upload their models to a base station co-located with an edge server for global model aggregation. However, given the limited transmit power, clients far from a base station may fail to upload models or suffer from low uplink data rate due to the severe path loss. To offer seamless services in a large region, wireless mesh network is a cost-effective and fast deployment choice. Compared with a single cell site, wireless mesh network can bring significant advantages like larger coverage, higher spectrum efficiency, and more adaptive/flexible network reconfigurability, which is deemed an important component of 5G/6G [9], [10]. In emerging heterogeneous networks (HetNets), multi-tier network entities, including macro/small base stations and relay stations, can naturally form a mesh of multi-hop wireless network [11]-[14]. In such a case, a macro base station can serve as the gateway base station (GBS), while the remaining network entities can be wirelessly interconnected to extend the coverage of the macro base station.

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Implementing FL in wireless mesh networks opens some unique research opportunities. A key observation about FL is that, a central server is only interested in the aggregated model, and hence it may be unnecessary to transmit every local model to the central site if they can be aggregated beforehand. By leveraging in-network edge computing resource, a multi-hop network can perform model aggregation at each intermediate router before sending data to the next hop. This process, called "in-network aggregation" in this paper, can significantly reduce the outgoing data traffic from routers, and hence enable more efficient model aggregation over multi-hop networks under limited communication resources.

Fully exploiting the potential of in-network aggregation requires a holistic system design for multi-hop wireless networks. First of all, judicious spectrum allocation is required to mitigate network-wide wireless interference. Second, model routing must be optimized by considering model aggregation, which is completely different from traditional flow optimization problem with flow conservation (e.g., ingoing flow equals outgoing flow at intermediate routers). At last, one should

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determine when to aggregate the models at each router by considering the communication and computing capabilities. These three issues are tightly intertwined, making the problem highly challenging. To tackle these challenges, in this paper, we jointly optimize spectrum allocation, routing, and innetwork aggregation to accelerate FL training over wireless mesh networks. To our best knowledge, FL over wireless mesh networks has seldom been studied. The closest work to ours is [15], where multi-agent reinforcement learning is employed to accelerate the FL convergence over wireless mesh networks by learning a routing strategy to minimize the average end-to-end model transmission delay. However, in-network aggregation has not been considered in their work. Besides, they devise a routing scheme operating on contentionbased wireless technology (e.g., 802.11 protocols), whereas we aim to design a centralized joint routing and spectrum allocation strategy by taking full advantage of the global knowledge of GBS.

The major contributions of this paper are summarized as follows.

- We propose an FL framework over wireless mesh networks with in-network aggregation. Specifically, our protocol sets a deadline for model download, update, and upload in each training round, and aims to maximize the aggregated models before the deadline. This objective is based on the observation that selecting more clients in each round can improve the training performance in FL [1], [16]. To fully reap the benefits of the multihop architecture, we jointly optimize routing, spectrum allocation, and in-network aggregation. As far as we know, this is the first FL framework over wireless mesh networks with in-network aggregation.
- We formulate our problem as a non-convex mixed-integer nonlinear programming, where the non-convexity arises from the in-network aggregation constraints. We transform the problem into a mixed-integer linear programming (MILP), and develop a coarse-grained fixing algorithm to obtain sub-optimal solution efficiently.
- Simulation results demonstrate the effectiveness of the proposed coarse-grained fixing algorithm by using the optimal solution to the formulated MILP as the benchmark, and show that in-network aggregation can significantly improve the training performance comparing to the counterpart without in-network aggregation.

The remainder of this paper is organized as follows. Section II introduces the related work. Section III presents the system architecture and federated learning training process. We formulate the optimization problem in Section IV, and offer the solution approach in Section V. In Section VI, we extend the formulation to consider traditional multi-hop relaying without in-network aggregation. Section VII conducts performance evaluation. We conclude the paper in the last section.

## II. RELATED WORK

A number of recent works investigate FL implementations over wireless networks. To reduce the training time to achieve a desired learning accuracy, client selection and radio resource management is the key. In [17], Chen et al. propose a joint learning and communication resource allocation scheme to minimize the FL loss by considering the packet errors introduced by wireless channels. In [18], Ren et al. develop a joint batchsize selection and communication resource allocation strategy for FL to optimize a novel criterion, called learning efficiency. In [19], Yang et al. address the joint communication and computing resource allocation problem for FL, with the objective to minimize the total energy consumption under latency constraint. In [16], Nishio et al. devise a client selection policy to aggregate as many model updates as possible within predefined deadline subject to the heterogeneous clients' computing and communication constraints. Unfortunately, all aforementioned works focus on FL implementation just for a single base station.

In FL, multi-level or multi-hop aggregation plays a pivotal role in increasing coverage and reducing the data traffic from a large set of clients [15], [20]-[24]. In [20], Liu et al. propose a two-level cloud-edge-client federated learning architecture and analyze its convergence property. Under similar two-level scenarios, the resource allocation problems are studied in [21] and [22]. In [23], Chen et al. propose a collaborative FL mechanism where local devices transmit models to nearby devices via device-to-device communications, and directly perform model aggregation on local devices. However, the above schemes focus on special or layered network structure, which cannot be applied to general mesh networks. Besides, routing has not been addressed in their works. In [15], Pinyoanuntapong et al. employ multi-agent reinforcement learning to learn the routing strategy to minimize the average end-toend model transmission latency over wireless mesh networks while failing to consider in-network aggregation and spectrum allocation.

The design of data aggregation scheme can be traced back to the studies on wireless sensor networks (WSNs). Analogous to FL, a sink node in a WSN may require an aggregated form of sensed data, e.g., temperature, where in-network computation can also greatly reduce the communication overhead. Similar to our work, the problem on maximizing the aggregated information within given deadline in WSNs has been addressed in several works [25], [26]. Unfortunately, the existing data aggregation schemes for WSNs cannot be applied to FL. First, FL has the crucial processes of global model download and local model update, which do not exist in the data aggregation problem for WSNs. Due to the heterogeneous channel conditions and computing resources of clients, the global model download and local model update times can be vastly different across clients, which greatly affect the optimal client/router selection, routing, and resource allocation strategy. Second, the existing schematic design on WSNs commonly ignores the in-network aggregation delay. This assumption may be reasonable for WSNs, since the operations on sensor information, e.g., temperature, is typically simple. Nevertheless, given the fact that state-of-the-art deep neural networks (DNNs) generally contain millions of parameters, innetwork aggregation delay is generally non-negligible in FL, which cannot be simply neglected.

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Fig. 1: Illustration of in-network aggregation over a toy mesh network. Each red underlined number represents a specific parameter of a client's model, and each bold number is the size of a client's dataset, i.e.,  $d_c = |\mathcal{D}_c|$ . Although an ML model is composed of many parameters, we just take one parameter, i.e., the red underlined number, for the ease of exposition. Each  $PoC^2$  sums up its received models before sending to the next hop. GBS sums up all the received models and divides the aggregated model by the total number of data samples.

## III. SYSTEM MODEL

### A. Federated Learning and In-network Aggregation

Assume that we have a set C of clients with local datasets  $\mathcal{D}_c$  for  $c \in C$  in the considered region. An FL server aims to train a global model using the data available at these clients. Considering supervised ML, a training data sample j consists of input sample  $x_j$  and label  $y_j$ . Let  $l_j(\theta) \triangleq l(\theta, x_j, y_j)$  represent the loss function on data sample j based on model  $\theta$ . For client  $c \in C$ , the loss function on its dataset  $\mathcal{D}_c$  is given by

$$L_c(\boldsymbol{\theta}) \triangleq \frac{1}{|\mathcal{D}_c|} \sum_{j \in \mathcal{D}_c} l_j(\boldsymbol{\theta}).$$
 (1)

The global loss function over all the local datasets is defined as

$$L(\boldsymbol{\theta}) \triangleq \frac{1}{|\mathcal{D}|} \sum_{c \in \mathcal{C}} |\mathcal{D}_c| L_c(\boldsymbol{\theta}), \qquad (2)$$

where  $\mathcal{D} \triangleq \bigcup_{c \in \mathcal{C}} \mathcal{D}_c$ .

To minimize the global loss function  $L(\theta)$ , the standard federated learning algorithm FedAvg proceeds iteratively as follows [1]. In each training round, each client downloads the global model from the central server. Each client updates the model based on its local dataset for several epochs, typically relying on gradient-descent algorithms, and then uploads the model to the central server. Upon receiving all the desired model updates, the central server sets the global model to the weighted average of these models:

$$\boldsymbol{\theta} = \frac{1}{|\mathcal{D}|} \sum_{c \in \mathcal{C}} |\mathcal{D}_c| \boldsymbol{\theta}_c, \tag{3}$$

where  $\theta_c$  represents the local model updated by client *c*. In practice, it may not be feasible to select all the clients in the every training round because of the limited communication and



Fig. 2: Federated learning over multi-hop wireless networks.  $t_{\text{cast}}$  is the model multicasting time, and  $\tilde{t}_m$  is the  $PoC^2$  m's update time (explained in Section III-C).

computing resource as well as clients' activities. Defining S as the set of selected clients in the considered round, the global model can still be updated according to (3) by aggregating only the models from the selected clients, i.e., replacing C with S and letting  $\mathcal{D} \triangleq \bigcup_{c \in S} \mathcal{D}_c$  in (3).

Since the central server is interested in the model average rather than each individual model update, a multi-hop network can aggregate the models in each intermediate router to reduce the data traffic. Specifically, client c can scale up the model update to  $|\mathcal{D}_c|\boldsymbol{\theta}_c$ , and upload to the associated router. Each router aggregates the received models, from clients and other routers, into one model by summing up the model parameters, then forwards to the next hop. Finally, the central server aggregates the models from routers, and scales the aggregated model by  $\frac{1}{|\bigcup_{c \in S} \mathcal{D}_c|} = \frac{1}{\sum_{c \in S} |\mathcal{D}_c|}$  to recover (3). While an ML model is composed of many parameters, we can take one parameter as an example for ease of exposition. Suppose that the central server desires the weighted average  $\frac{d_{1}*1+d_{2}*2+d_{3}*3+d_{4}*4+d_{5}*5}{d_{1}+d_{2}+d_{3}+d_{4}+d_{5}} = \frac{18}{6} = 3 \text{ from five clients holding}$ parameter 1, 2, 3, 4, and 5, respectively, where  $d_{1} = 1, d_{2} = 1$ ,  $d_3 = 2, d_4 = 1$ , and  $d_5 = 1$  are the sizes  $|\mathcal{D}_c|$  of clients' local datasets. As illustrated in Fig. 1, the central server can exactly recover the desired result 3 via in-network aggregation over the toy mesh network.

#### B. Network Architecture

Let us consider a static wireless mesh network with one G-BS g and a set  $\mathcal{R}$  of wireless routers, as shown in Fig. 2. These routers, also called points of communication and computing  $(PoC^2s)$ , are set-top like devices endowed with customized communication (e.g., software-defined radio), computing, and

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Notation	Description
$PoC^2$	Point of communication
	and computing

 $\mathcal{D}_{c}$ 

The dataset of client c

TABLE I: Frequently used nomenclature and notations

$\mathcal{R}$	The set of $PoC^2$ s
$\mathcal{S}_m$	The clients selected by $PoC^2 m$
g	The gateway base station (GBS)
$\mathcal{B}_m$	The set of backhaul channels
	around node m
W	The bandwidth for each
	backhaul channel
$W_{\rm cast}$	The bandwidth for the downlink
	multicast channel
$\Gamma_m$	The transmission set of $PoC^2 m$
$\mathcal{I}_m$	The interference set of $PoC^2 m$
$c_m/c_g$	The time taken by $PoC^2 m/\text{GBS}$
	to sum up two models
$e_{m,n}$	The capacity of a channel
	over link $(m, n)$
${ ilde t}_m$	The time for $PoC^2$ m to collect and
	aggregate set $\mathcal{S}_m$ of clients' models
D	The length of a training round
$\Delta$	The length of a control interval
K	Number of control intervals
	in a training round
$a_m, r_{m,n}, s_{m,n}^{b,k},$	Decision variables
$f_{m,n}^{b,k}, t_m, t^{\text{cast}}$	(explained in Section IV)
$v_m^k,  h_n^k,  y_{m,n}, \ b_m^k,  d_n^k,  u_{m,n}$	Auxiliary variables (to linearize P1)

storage capabilities, or CCS capabilities for short. GBS is typically a macro base station endowed with significantly CCS capabilities for global model aggregation. GBS also acts as a central controller to coordinate  $PoC^2$ s for model delivery and aggregation via multi-hop wireless links.

At the beginning of each training round, GBS multicasts a global model to a set of clients for model training. After local training at client side,  $PoC^2s$  aggregate models from their associated clients and then deliver the models to GBS via multi-hop relaying. Each  $PoC^2$  aggregates models from its associated clients and other  $PoC^2$ s before sending to the next hop, which is the in-network aggregation process. The clients,  $PoC^2$ s, and GBS are wirelessly interconnected. However, we assume that the backhaul links (among  $PoC^2$ s and GBS) and access links (from clients to  $PoC^2$ s) use different set of channels, and hence do not interfere with each other. Moreover, we assume that each client is pre-associated with one  $PoC^2$ . In this way, we can concentrate on the multi-hop wireless backhauling in this study, while excluding clients and access links from our network topology. We want to first add some explanations for the nodes ( $PoC^2$ s and GBS), links, and channels in the wireless backhaul part as follows. Let  $\mathcal{B}_m$  represent the set of channels available around node  $m \in \{g\} \cup \mathcal{R}$ , and (m, n) denote the uplink wireless link from node  $m \in \mathcal{R}$  to node  $n \in \{g\} \cup \mathcal{R}$ . The channels in  $\mathcal{B}_m \cap \mathcal{B}_n$  can be utilized to support model transmission between node m and node n. Since the downlink multicasting from GBS to clients is carried out before model upload, it does not interfere with  $\mathcal{B}_m$  around each  $PoC^2$  for model upload. Thus, we do not need to specify the channel used by GBS for downlink multicasting, but rather simply assume that the multicast bandwidth is  $W_{\text{cast}}$ .

By adopting the deterministic power propagation model, we characterize the channel gain for link (m, n) on channel b as  $\gamma_{m,n} = \eta d_{m,n}^{-\alpha}$ , where  $\eta$  is an antenna related constant,  $d_{m,n}$  is the distance between node m and node n, and  $\alpha$  is the path loss exponent [27]<sup>1</sup>. Each channel is assumed to be additive white Gaussian noise (AWGN) channel with fixed noise power. Since all transmitted data is assumed to be the models of the same size for the analysis, we can treat a model as the basic unit of the transmitted data in our systems. Therefore, we normalize channel capacity and other parameters related to data rate/amount by model size M for notational convenience. The normalized capacity of a channel over link (m, n) is given by

$$e_{m,n} = \frac{W}{M} \log\left(1 + \frac{\gamma_{m,n}p}{WN_0}\right),\tag{4}$$

where W is the bandwidth of each channel, p is  $PoC^{2}$ 's transmit power on each channel,  $N_{0}$  is the noise power spectral density, and M is the ML model size. We denote by  $\Gamma_{m}$  and  $\mathcal{I}_{m}$  the transmission set and interference set of  $PoC^{2}$ m, respectively, where  $\Gamma_{m}$  and  $\mathcal{I}_{m}$  contain the nodes within a transmission range R and a potentially larger interference range R' of  $PoC^{2}$ m. Following the well-known protocol interference model [28], we assume that link (m, n) exists only if node n is in  $\Gamma_{m}$ , and the interference from node m to node n exists only if node n is in  $\mathcal{I}_{m}$ . For readers' convenience, the frequently used notations are summarized in Table I.

#### C. Federated Learning Training Process

We next present our FL training process, which consists of multiple training round. Each training round involves four stages, i.e., coordination, model download,  $PoC^2$  update, and model upload.

In the coordination stage, GBS collects the channel state information (CSI) for wireless backhaul links (m, n), downlink channels to clients (for downlink multicasting), and the available computing resource at each  $PoC^2$  (for measuring innetwork aggregation delay). Meanwhile, each  $PoC^2$  collects the information about its associated clients, including their CSI and available computing resource. Based on the information, each  $PoC^2 m$  computes the set  $S_m$  of selected clients, and the needed time  $\tilde{t}_m$  for collecting and aggregating these clients' models (called  $PoC^2$  update time), and reports  $S_m$  and  $\tilde{t}_m$  to GBS. Finally, GBS makes the centralized coordination (e.g.,  $PoC^2$  selection, routing, and link scheduling) and informs the decisions to  $PoC^2s$  for execution. Due to heterogeneous computing and communication resources at  $PoC^2s$ , as depicted in Fig. 2.

<sup>1</sup>For simplicity, we assume the same gain model for all channels.

A key process above is that a  $PoC^2$  needs to compute  $S_m$  and  $\tilde{t}_m$ . By assuming that proximate  $PoC^2$ s are assigned with different access bands and thus do not interfere with each other when collecting models from clients, each  $PoC^2$  can implement some existing single-cell FL policies to obtain  $S_m$  and  $\tilde{t}_m$ . For instance, the FedCS protocol proposed in the well-cited paper [16], allowing a  $PoC^2$  to aggregate as many models as possible before a predefined deadline, can be adopted here to obtain  $S_m$  and  $\tilde{t}_m$ .

In the model download stage, GBS multicasts the global model to the *selected clients*. Note that our policy will only select  $PoC^2$ s, each of which has the autonomy of selecting clients to update and upload models based on its local situations. Therefore, the selected clients are those selected by the *selected PoC*<sup>2</sup>s. In other words, any client associated with the unselected  $PoC^2$ s would not participate or receive the global model in the current round. In addition, we have made the implicit assumption that clients are in the downlink coverage of GBS. Given the fact that a GBS typically has powerful communication capabilities (e.g., high transmit power), we believe that this assumption is reasonable in many cases.

In the  $PoC^2$  update stage, the set  $S_m$  of selected clients perform local model update and upload the models to  $PoC^2$ m. Then, each  $PoC^2$  aggregates the received clients' models. As discussed before, some existing single-cell FL protocols can be used at this stage.

In the model upload stage, the  $PoC^2$ s collaboratively deliver their aggregated models to GBS. Upon receiving the models from other  $PoC^2$ , a  $PoC^2$  performs model aggregation before sending to the next hop. Note that the unselected  $PoC^2$ s could also facilitate the multi-hop model delivery, even though they do not directly collect models from clients.

## IV. PROBLEM FORMULATION

Since the aforementioned four stages in one training round will be repeated until the global model converges to a desired accuracy, we focus on one training round for analysis. In each round, being consistent with [16], [29], our design goal is to aggregate as many model updates as possible at GBS given a predefined deadline D and resource constraints. This objective is motivated by the key observation that increasing the number of participating clients can accelerate the training process in FL [1], [16], [29]–[31].

We start by introducing the network resource constraints. Since ML models are gradually moved from source nodes to GBS, the link traffic demands are not static over time, implying that a static resource allocation strategy may not be able to fully exploit the network resources. Therefore, we assume that a training round consist of K control intervals, and different resource allocations can be made across the control intervals to accommodate the time-varying traffic. We define resource tuple ((m, n), b, k) to indicate that over link (m, n), transmitter m operates on channel b during the k-th control interval. For clarity, the decision variables and definitions are summarized below.

•  $a_m \in \{0, 1\}$  is the  $PoC^2$  selection variable, where  $a_m = 1$  if  $PoC^2 m$  is selected, and 0 otherwise. As explained

before, a selected  $PoC^2$  will collect its clients' models, whereas an unselected  $PoC^2$  will not.

- $r_{m,n} \in \{0,1\}$  is the routing decision variable, where  $r_{m,n} = 1$  if  $PoC^2 m$  forwards the data to node  $n (PoC^2 \text{ or GBS})$ , and 0 otherwise.
- $s_{m,n}^{b,k} \in \{0,1\}$  denotes the resource allocation strategy, where  $s_{m,n}^{b,k} = 1$  if resource tuple ((m,n), b, k) is active, and 0 otherwise.
- f<sup>b,k</sup><sub>m,n</sub> ≥ 0 represents the amount of data flow (normalized by model size) delivered via resource tuple ((m, n), b, k).
- $t_m \in [0, D]$  indicates the aggregation time that node  $m (PoC^2 \text{ or GBS})$  stops receiving models from other  $PoC^2$ s and begins in-network aggregation.
- $t^{\text{cast}} \in [0, D]$  represents the time for downlink model multicasting.

We will use boldfaced a, r, s, f, and t to denote the collections of  $a_m, r_{m,n}, s_{m,n}^{b,k}, f_{m,n}^{b,k}$ , and  $t_m$ , respectively.

## A. Routing Constraints

For simplicity, we study a single-path routing scheme where a node can have at most one outgoing link [32]. In other words, a  $PoC^2$  cannot partition its aggregated model into multiple data pieces for sending to multiple receivers<sup>2</sup>. We have

$$\sum_{n\in\Gamma_m} r_{m,n} \le 1, \forall m \in \mathcal{R}.$$
(5)

Besides,  $PoC^2 m$  must transmit if receiving the models from other  $PoC^2$ s or selected by GBS ( $a_m = 1$ ), leading to

$$\sum_{n\in\Gamma_m} r_{m,n} \ge r_{m',m}, \quad \forall m \in \mathcal{R}, m' \in \{m' | m \in \Gamma_{m'}\}, \quad (6)$$
$$\sum_{n\in\Gamma_m} r_{m,n} \ge a_m, \quad \forall m \in \mathcal{R}. \quad (7)$$

For the sake of simplicity, we omit the constraint on storage by assuming that each  $PoC^2$  has enough storage space to cache the received models for aggregation. Since  $PoC^2 m$ aggregates the received models (from clients and/or other  $PoC^2$ s) into one model before transmitting to the next hop, the outgoing link (m, n) must deliver exactly one model over the total K control intervals if routing decision  $r_{m,n} = 1$  is made, yielding

$$\sum_{b \in \mathcal{B}_m \cap \mathcal{B}_n} \sum_{k=1}^K f_{m,n}^{b,k} = r_{m,n}, \quad \forall m \in \mathcal{R}, n \in \Gamma_m, \quad (8)$$

where the flow amount  $f_{m,n}^{b,k}$  is normalized by model size.  $f_{m,n}^{b,k}$  is constrained by spectrum allocation and aggregation time decisions for node m and n, which will be introduced in the next subsection. (8) also ensures that there is no "routing loop", as the flow amount  $f_{m,n}^{b,k}$  (and therefore  $r_{m,n}$ ) can be positive only if aggregation time  $t_n > t_m$ , as can be seen later. Since there is no loop in a route and only GBS g is not required to transmit after receiving models, all the models from selected  $PoC^2$ s can be eventually transferred to GBS.

<sup>2</sup>While multi-path routing may take advantage of load balancing to improve throughput, it would introduce more complexity when taking in-network aggregation into account. Hence, we will not investigate it in this paper.

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#### B. Aggregation Time and Flow Constraints

At the beginning, GBS multicasts a global model to a set of clients. To enable multicasting, GBS should employ the modulation and coding scheme in accordance with the client experiencing the worst propagation condition. Let  $e_m^{\rm DL}$  be the normalized downlink channel capacity (normalized by model size M) from GBS to the weakest client (with the lowest downlink signal-to-noise ratio (SNR)) in  $S_m$ , i.e.,

$$e_m^{\rm DL} = \frac{W_{\rm cast} \log \left(1 + \frac{\min_{c \in S_m} \{\gamma_{g,c}\}P}{W_{\rm cast}N_0}\right)}{M},\tag{9}$$

where  $\gamma_{g,c}$  is the channel gain from GBS to client c, P is GBS's downlink transmit power, and  $W_{\text{cast}}$  is the multicasting bandwidth. Since multicasting is carried out before model upload, GBS can re-utilize the backhaul channels to conduct the downlink transmissions. In this case, we have  $W_{\text{cast}} = W|\mathcal{B}_g|$ , recalling that  $\mathcal{B}_g$  is the set of channels available for GBS, and W is the channel bandwidth. Furthermore, the multicasting time  $t^{\text{cast}}$  is determined by the weakest client among all the clients selected by different  $PoC^2$ s, yielding

$$t^{\text{cast}} \ge \frac{1}{e_m^{\text{DL}}} a_m, \quad m \in \mathcal{R}.$$
 (10)

Thus,  $t^{\text{cast}}$  depends on  $PoC^2$  selection variables  $a_m$ .

After receiving the global model, local update is performed by each  $PoC^2$ .  $PoC^2 m$ , if selected by the system, should receive the models from  $|S_m|$  clients, and aggregate these local models into one model, which demands  $\tilde{t}_m$  (i.e.  $PoC^2$  update time) in total. Consequently, the aggregation time  $t_m$  for  $PoC^2$ m must satisfy

$$t_m \ge t^{\text{cast}} + \tilde{t}_m a_m, \quad m \in \mathcal{R}.$$
 (11)

We use in-network aggregation delay  $\sigma_m(a, r)$  to denote the backhaul-level model aggregation delay (not including the time  $PoC^2$  m aggregates the local models from  $S_m$ , which has already been considered in  $\tilde{t}_m$ ), i.e.,

$$\sigma_m(\boldsymbol{a}, \boldsymbol{r}) = \left(\sum_{\{m' \mid m \in \Gamma_{m'}^I\}} r_{m',m} + a_m - 1\right)^+ c_m, \quad \forall m \in \mathcal{R}$$
(12)

where  $c_m$  represents the computation delay for summing up two models, and  $x^+$  denotes the positive part of x, i.e.,  $\max\{x, 0\}$ . The number of models received by  $PoC^2 m$ is equal to  $\sum_{\{m'|m\in\Gamma_{m'}\}} r_{m',m} + a_m$ , i.e., the number of routing decisions made towards it, plus one if the  $PoC^2$  is selected (i.e., plus the aggregated local model). The number of summations is equal to the number of received models minus one. The positive part operator  $x^+$  ensures that  $\sigma_m(a, r) = 0$ if node m receives no model.

Since a  $PoC^2$  aggregates all received models into one model, there is no benefit for it to transmit before completing the aggregation. Therefore,  $PoC^2 m$  is allowed to transmit only after completing in-network aggregation, namely, after  $t_m + \sigma_m(a, r)$ . Moreover, link (m, n) cannot carry data flow after  $t_n$ , i.e., the time that receiver n stops receiving models. These conditions impose the following constraints on how much data traffic can be carried over each resource tuple:

$$f_{m,n}^{b,k} \le s_{m,n}^{b,k} e_{m,n} \Delta, \tag{13}$$

$$f_{m,n}^{b,k} \le e_{m,n} \Big( \Delta k - \big( t_m + \sigma_m(\boldsymbol{a}, \boldsymbol{r}) \big) \Big)^+, \qquad (14)$$

$$f_{m,n}^{b,k} \le e_{m,n} (t_n - \Delta(k-1))^+,$$
 (15)

$$f_{m,n}^{b,k} \le e_{m,n} \Big( t_n - \big( t_m + \sigma_m(\boldsymbol{a}, \boldsymbol{r}) \big) \Big)^+,$$
 (16)

$$\forall m \in \mathcal{R}, n \in \Gamma_m, b \in \mathcal{B}_m \cap \mathcal{B}_n, k \in \{1, ..., K\}.$$

As indicated in (13), the data flow  $f_{m,n}^{b,k}$  is upper bounded by  $e_{m,n}\Delta$  if the resource tuple  $s_{m,n}^{b,k}$  is allocated, i.e.,  $s_{m,n}^{b,k} = 1$ , and 0 otherwise, where  $e_{m,n}$  is the link capacity given in (4) and  $\Delta$  is the length of the k-th control interval  $[(k-1)\Delta, k\Delta]$ . Moreover,  $f_{m,n}^{b,k}$  is further constrained by time  $t_m + \sigma_m(a, r)$  and  $t_n$ , since the transmission can only be conducted between these two time instants. Overall, (13)-(16) together ensure that the data transmissions over resource tuple  $s_{m,n}^{b,k}$  can only be conducted during the intersection of the k-th control interval  $[(k-1)\Delta, k\Delta]$  and the time interval  $[t_m + \sigma_m(a, r), t_n]$ .

During the model upload stage, GBS does not transmit any models. Therefore, the optimal  $t_g$  (for stopping receiving models) can be set to the deadline D minus the time that it should take to perform global aggregation:

$$t_g = D - \bar{c} - \left(\sum_{\{m' \mid g \in \Gamma_{m'}\}} r_{m',g} - 1\right)c_g,$$
 (17)

where  $\overline{c}$  is the time taken by GBS to scale the aggregated model by  $\frac{1}{\sum_{c \in S} |\mathcal{D}_c|}$ , and  $c_g$  is the time for GBS to sum up two models. The last term indicates that the number of summation operations will be equal to the number of received models minus one, if GBS receives at least one model (which is the non-trivial case).

#### C. Resource Allocation Constraints

The aforementioned routing and in-network aggregation rely on appropriate network resource allocation. In our formulation, the resource allocation strategy is characterized by the timefrequency resource tuples  $s_{m,n}^{b,k}$ . Due to the conflict relationship, not all the resource tuples can be chosen together. A node is not allowed to either receive from or transmit to multiple nodes on the same channel in an interval, which is expressed as

$$\sum_{\substack{\{n\in\Gamma_{m}|b\in\mathcal{B}_{n}\}\\ \sum_{\{m'|m\in\Gamma_{m'},b\in\mathcal{B}_{m'}\}}} s_{m',m}^{b,k} \leq 1,$$

$$\forall m\in\mathcal{R}\cup\{g\}, b\in\mathcal{B}_{m}, k\in\{1,...,K\},$$
(18)
(18)
(19)

To avoid self-interference, a  $PoC^2$  cannot use a single channel for transmission and reception simultaneously, yielding

$$s_{m',m}^{b,k} + \sum_{\{n \in \Gamma_m | b \in \mathcal{B}_n\}} s_{m,n}^{b,k} \le 1, \forall m \in \mathcal{R}, \\ b \in \mathcal{B}_m, m' = \{m' | m \in \Gamma_{m'}, b \in \mathcal{B}_{m'}\}, k \in \{1, ..., K\}.$$
(20)

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A feasible scheduling should also ensure that there is no interference (in the sense of the protocol interference model) among the nodes. Specifically, if  $PoC^2 m$  is transmitting to node n, other  $PoC^2$ s that have node n within their interference ranges cannot use the same channel and time resource. We therefore have

$$s_{m,n}^{b,k} + \sum_{\{n' \in \Gamma_{m'} | b \in \mathcal{B}_{n'}\}} s_{m',n'}^{b,k} \le 1,$$
  
$$\forall m \in \mathcal{R}, n \in \Gamma_m, b \in \mathcal{B}_m \cap \mathcal{B}_n, m' \in \Upsilon_n^b, k \in \{1, ..., K\},$$
(21)

where  $\Upsilon_n^b = \{m' \in \mathcal{R} | n \in \mathcal{I}_{m'}, b \in \mathcal{B}_{m'}, m' \neq m\}$  denotes the set of  $PoC^2$ s having receiver n within their interference ranges and with channel b available.

In summary, given the constraints above, our optimization problem, which jointly optimizes resource allocation  $s_{m,n}^{b,k}$ , routing decision  $r_{m,n}$ ,  $PoC^2$  selection  $a_m$ , flow allocation  $f_{m,n}^{b,k}$ , multicasting time  $t^{\text{cast}}$ , and node aggregation time  $t_m$ , is formulated as follows

$$\mathbf{P1:} \max_{\boldsymbol{a},\boldsymbol{r},\boldsymbol{s},\boldsymbol{f},\boldsymbol{t},\boldsymbol{t}^{\text{cast}}} \sum_{m \in \mathcal{R}} w_m a_m, \\ s.t. \quad (5) - (21), \\ s_{m,n}^{b,k} \in \{0,1\}, f_{m,n}^{b,k} \ge 0, \quad \forall m \in \mathcal{R}, \\ n \in \Gamma_m, b \in \mathcal{B}_m \cap \mathcal{B}_n, k \in \{1,...,K\},$$
(22)

$$r_{m,n} \in \{0,1\}, \ \forall m \in \mathcal{R}, n \in \Gamma_m, \quad t_m \in [0,D], \ \forall m \in \mathcal{R}, t^{\text{cast}} \in [0,D], \quad \forall m \in \mathcal{R},$$

$$(23)$$

where  $w_m = \frac{\sum_{c \in S_m} |\mathcal{D}_c|}{\sum_{c \in S} |\mathcal{D}_c|}$  is the weighting factor for  $PoC^2 m$ , which is proportional to the number of data samples associated with  $PoC^2 m$ . Due to the non-convex constraints (14)-(16) on aggregation time, Problem **P1** is a non-convex mixed-integer nonlinear programming, for which we have the following result.

Theorem 1: Problem P1 is NP-hard.

Proof: See Appendix A.

Briefly speaking, it can be shown that the maximum independent set problem can be reduced to Problem **P1**. It has been proved that the maximum independent set problem is not only NP-hard but also extremely hard to approximate [33]<sup>3</sup>. This fact hinders us from not only finding the exact solution, but also a constant-factor approximation to Problem **P1** in polynomial time. Therefore, we will develop a heuristic solution approach to Problem **P1**.

## V. SOLUTION APPROACH

In this section, we first transform the mixed-integer nonlinear programming into a mixed-integer linear programming (MILP). Then, inspired by [34], [35], we develop a heuristic algorithm, called coarse-grained fixing procedure, to effectively find the solution.

 ${}^{3}$ Reference [33] studies the maximum clique problem, which is approximation-equivalent to the maximum independent set problem. These two problems are complementary because a clique in a graph is an independent set of the complement graph.

#### A. Linearization

The main challenge in solving Problem **P1** stems from the non-convex constraints (14)-(16) with positive part operator "+" and a nonlinear function  $\sigma_m(a, r)$  (defined in (12)). To linearize these constraints, we first need to linearize  $\sigma_m(a, r)$ , for which we can directly remove the positive part operator "+" as follows

$$\sigma_m(\boldsymbol{a}, \boldsymbol{r}) = \left(\sum_{\{m'|m\in\Gamma_{m'}\}} r_{m',m} + a_m - 1\right) c_m, \quad \forall m \in \mathcal{R}.$$
(24)

Although  $\sigma_m(\boldsymbol{a}, \boldsymbol{r})$  can be  $-c_m$  based on the linear constraint (24), which is not meaningful in practice, it would not impact the solution. This is because a  $PoC^2$  with  $\sigma_m(\boldsymbol{a}, \boldsymbol{r}) = -c_m$  would never receive or forward any model (since  $r_{m',m}$  and  $a_m$  are equal to 0), and hence have no impact on the system.

In order to linearize (14)-(16), we also need to remove the operator "+" in (14)-(16). We define several auxiliary variables, including continuous variables  $v_m^k \in [0, D]$ ,  $h_n^k \in [0, D]$ , and  $y_{m,n} \in [0, D]$ , and binary variables  $b_m^k$ ,  $d_n^k$ , and  $u_{m,n}$ . Then, (14)-(16) can be equivalently expressed as

$$f_{m,n}^{b,k} \le e_{m,n} v_m^k, \ f_{m,n}^{b,k} \le e_{m,n} h_n^k, \ f_{m,n}^{b,k} \le e_{m,n} y_{m,n}, \ (25) 
 \forall m \in \mathcal{R}, n \in \Gamma_m, b \in \mathcal{B}_m \cap \mathcal{B}_n, k \in \{1, ..., K\}.$$

with

$$v_{m}^{k} \geq k\Delta - (t_{m} + \sigma_{m}(\boldsymbol{a}, \boldsymbol{r})),$$

$$v_{m}^{k} \leq k\Delta - (t_{m} + \sigma_{m}(\boldsymbol{a}, \boldsymbol{r})) + Db_{m}^{k}, v_{m}^{k} \leq D(1 - b_{m}^{k}),$$

$$v_{m}^{k} \in [0, D], b_{m}^{k} \in \{0, 1\}, \forall m \in \mathcal{R}, k \in \{1, ..., K\}, \quad (26)$$

$$h_{n}^{k} \geq t_{n} - \Delta(k - 1), h_{n}^{k} \leq t_{n} - \Delta(k - 1) + Dd_{n}^{k},$$

$$h_{n}^{k} \leq D(1 - d_{n}^{k}), h_{n}^{k} \in [0, D],$$

$$d_{n}^{k} \in \{0, 1\}, \quad \forall n \in \mathcal{R} \cup \{g\}, k \in \{1, ..., K\}, \quad (27)$$

$$y_{m,n} \geq t_{n} - (t_{m} + \sigma_{m}(\boldsymbol{a}, \boldsymbol{r})),$$

$$y_{m,n} \leq t_{n} - (t_{m} + \sigma_{m}(\boldsymbol{a}, \boldsymbol{r})) + Du_{m,n},$$

$$y_{m,n} \leq D(1 - u_{m,n}), \quad y_{m,n} \in [0, D], \quad u_{m,n} \in \{0, 1\},$$

$$\forall m \in \mathcal{R}, n \in \Gamma_{m}. \quad (28)$$

The linearization is achieved at the cost of adding three binary variables  $b_m^k$ ,  $d_n^k$ , and  $u_{m,n}$ . Enforced by (26), (27), and (28), the auxiliary variable  $v_m^k$ ,  $h_n^k$ , and  $y_{m,n}$  are equal to the term ()<sup>+</sup> in (14)-(16), respectively. Consequently, Problem **P1** can be reformulated by replacing (12) and (14)-(16) with the linear constraints above, i.e.,

P2: 
$$\max_{\boldsymbol{a},\boldsymbol{r},\boldsymbol{s},\boldsymbol{f},\boldsymbol{t},\boldsymbol{t}^{\text{cast}},\boldsymbol{v},\boldsymbol{h},\boldsymbol{y},\boldsymbol{b},\boldsymbol{d},\boldsymbol{u}} \sum_{m \in \mathcal{R}} w_m a_m,$$
  
s.t. (5) - (11), (13), (17) - (28),

where v, h, y, b, d, and u denote the collections of the auxiliary variables  $v_m^k$ ,  $h_n^k$ ,  $y_{m,n}$ ,  $b_m^k$ ,  $d_n^k$ , and  $u_{m,n}$ . Since **P2** is a reformulation of **P1**, it is not hard to see that the proof for NP-hardness in Theorem 1 can also be applied to **P2**. Fortunately, **P2** is an MILP, implying that many existing algorithms, such as branch and bound algorithm, or off-the-shelf

Algorithm 1 Coarse-grained Fixing Procedure

**Input:** The parameters for Problem **P2** and threshold  $\theta$ . **Output:** The solution *x* to Problem **P2**.

- 1: For Problem **P2**, eliminate the nodes in set  $\Gamma_m$  farther from GBS than node m is if  $\Gamma_m$  is not empty after this elimination.
- 2: Relax  $s_{m,n}^{b,k}$  to [0,1] in **P2**. 3: while not all  $s_{m,n}^{b,k}$  are fixed do
- Solve the relaxed **P2** with fixed  $s_{m,n}^{b,k}$  (if any), and obtain 4: the solution for  $s_{m,n}^{b,k}$ .
- if there exists  $s_{m,n}^{b,k} > \theta$  then 5:
- Fix all  $s_{m,n}^{b,k} > \theta$  to 1. 6:
- else 7:
- Fix the largest  $s_{m,n}^{b,k}$  to 1. 8:
- 9: end if
- Based on the fixed  $s_{m,n}^{b,k}$ , fix some other  $s_{m,n}^{b,k}$  to 0 10: according to (18)-(21).
- 11: end while
- 12: Solve Problem **P2** with fixed  $s_{m,n}^{b,k}$  to obtain the solution x.

Algorithm	2	Enhanced	Coarse-grained	Fixing	Procedure
0			U	0	

Input: The parameters for Problem P2, scale factors  $\{\beta_1, \beta_2, ..., \beta_N\}$ , and threshold  $\theta$ .

**Output:** The solution x to Problem **P2**.

- 1: For Problem **P2**, eliminate the nodes in set  $\Gamma_m$  farther from GBS than node m is if  $\Gamma_m$  is not empty after this elimination.
- 2: Initialize i = 0.
- 3: for i < N do
- i = i + 1.4:
- Change link capacity  $e_{m,n}$  to  $\beta_i e_{m,n}$ . 5:
- Execute line 1 11 in Algorithm 1 to fix  $s_{m,n}^{b,k}$ . 6:
- Solve Problem **P2** with the original link capacity  $e_{m,n}$ 7: and the fixed  $s_{m,n}^{b,k}$  to obtain the solution  $z_i$  and the objective value  $V_i$ .
- 8: end for
- 9:  $x = z_{\arg \max_{1 \le i \le N} \{V_i\}}$ .

softwares (e.g., MATLAB) can solve it exactly in practice. However, these approaches may not be applicable to a largescale problem, because the time complexity exponentially increases with the number of the integer variables, particularly the four-dimension resource allocation variables  $s_{m,n}^{b,k}$ . In view of this, we further devise a heuristic for more efficient solution finding.

# B. Coarse-grained Fixing Procedure

1) Basic Coarse-grained Fixing Procedure: The major obstacle in solving Problem **P2** lies in the integer variables  $s_{m,n}^{b,k}$ , the number of which increases with the network size and resource dimensions. Our idea is to first develop a heuristic algorithm to fix  $s_{m,n}^{b,k}$ , and then solve the problem with fixed  $s_{m,n}^{b,k}$ . Specifically, we will fix  $s_{m,n}^{b,k}$  through an iterative process. At each round, we relax *all* the integer variables  $s_{m,n}^{b,k}$ ,

 $a_m, r_{m,n}, b_m^k, d_n^k$ , and  $u_{m,n}$  to [0, 1], converting Problem P2 into a linear programming (LP), which can be easily solved by LP solvers. Given the solution  $s_{m,n}^{b,k}$  to the relaxed problem, we fix all the  $s_{m,n}^{b,k} > \theta$  to 1, where the threshold  $\theta$  can be chosen from [0.5, 1]. The threshold range ensures that (18)-(21) will not be violated upon fixing  $s_{m,n}^{b,k}$ . If all  $s_{m,n}^{b,k}$  are less or equal to  $\theta$ , we set the largest  $s_{m,n}^{b,k}$  to 1. Besides, we fix some other  $s_{m,n}^{b,k}$  to 0 based on the conflict relationships characterized by (18)-(21). With fixed  $s_{m,n}^{b,k}$ , we repeatedly solve the resulting LP with decreasing number of variables until all  $s_{m,n}^{b,k}$  are fixed to either 0 or 1. Since at least one variable of  $s_{m,n}^{b,k}$  is fixed at each round, the iteration number of solving LP is limited by the number of  $s_{m,n}^{b,k}$ , implying that the iterative process can converge. However, the actual iteration number is much smaller than this, since multiple variables  $s_{m,n}^{b,k}$  can be fixed during one iteration. Finally, with the  $s_{m,n}^{b,k}$  in place, we solve the resulting optimization problem to obtain the solution. Note that, although variables  $s_{m,n}^{b,k}$  are fixed, at the last step, we still need to solve an MILP with binary variables  $a_m$ ,  $r_{m,n}$ ,  $b_m^k$ ,  $d_n^k$ , and  $u_{m,n}$ . However, the resulting MILP can be efficiently solved by off-the-shelf optimization software in practice (as validated in Section VII-B), because the number of integer variables is not large under a practical problem setting. The algorithm is summarized in Algorithm 1.

In addition, to reduce the complexity of the solution approach and forward models to GBS quickly, we eliminate some receivers in transmission set  $\Gamma_m$  of each node m to narrow down the decision space. Specifically, we eliminate the nodes in  $\Gamma_m$  which are farther from GBS than node m is if  $\Gamma_m$ does not become empty after this elimination (corresponding to Line 1 in Algorithm 1). The rationale is that forwarding data far away is typically not the optimal solution given that our objective is to deliver models to GBS.

2) Enhanced Coarse-grained Fixing Procedure: Although the approach above can yield a solution efficiently, it relies on a greedy fixing rule, which is not optimal. The suboptimality comes from the fact that the set of  $s_{m,n}^{b,k}$ , which are fixed to 1, may not be optimal. Enlightened by [34], we can obtain different sets of fixed  $s_{m,n}^{b,k}$ , and choose the best among them so as to enhance the solution. Specifically, we change the link capacity  $e_{m,n}$  of each channel by a scale factor  $\beta \in (0,1]$  and fix  $s_{m,n}^{b,k}$  accordingly. When  $e_{m,n}$  reduces to  $\beta e_{m,n}$ , the channel gain becomes lower. To support model delivery, the system may need to select more critical resource tuples, thereby producing a different set of fixed  $s_{m,n}^{b,k}$ . Then, with the fixed  $s_{m,n}^{b,k}$  in place, we solve the resulting problem with the *original* link capacity  $e_{m,n}$  to obtain the solution. This process can be done multiple times by using different scale factors. Assuming that we perform N trials with scale factors  $\{\beta_1, \beta_2, ..., \beta_N\}$ , the solution is set to the best among these N trials. Essentially, this process potentially improves the solution at the cost of running the coarse-grained fixing procedure multiple times. We call this procedure as "enhanced coarse-grained fixing procedure", and outline it in Algorithm 2.

#### VI. EXTENSION: TRADITIONAL MULTI-HOP RELAYING

For the benchmarking purpose, in this section, we adapt our problem formulation to consider the traditional multihop relaying scheme without in-network aggregation. In such a case, we assume that each  $PoC^2$  still aggregates its local models from set  $S_m$  of clients, while directly relaying other  $PoC^2$ s' models to the next hop upon receiving. Let  $\overline{f}_{m,n}^{b,k}$  denote the flow amount delivered via resource tuple ((m,n),b,k) accounting for the local aggregated model at  $PoC^2 m$ , which constitutes part of  $f_{m,n}^{b,k}$ . We have the flow conservation constraints

$$\sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{k_{0}} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) \leq \sum_{\{m' \mid m \in \Gamma_{m'}\}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m'}} \sum_{k=1}^{k_{0}} f_{m',m}^{b,k}, \ \forall m \in \mathcal{R},$$

$$\sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{n \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{n}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{b \in \mathcal{B}_{m} \cap \mathcal{B}_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{m \in \Gamma_{m}} \sum_{k=1}^{K} (f_{m,n}^{b,k} - \overline{f}_{m,n}^{b,k}) = \sum_{m \in \Gamma_{m}} \sum_{m \in \Gamma_$$

$$\sum_{\{m'|m\in\Gamma_{m'}\}}\sum_{b\in\mathcal{B}_m\cap\mathcal{B}_{m'}}\sum_{k=1}^{K}f_{m',m}^{b,k}, \ \forall m\in\mathcal{R}.$$
 (30)

Constraint (29) means that during the first  $k_0$  time slots, for  $PoC^2$  m, the outgoing data flow amount should be no more than the incoming data amount (from other  $PoC^2$ ) plus its local aggregated model.  $PoC^2$  m can temporarily store some incoming flow and transmit in the upcoming control intervals, as indicated in (29). Constraint (30) guarantees the flow balance over the whole training round that spans K intervals. For simplicity, we do not consider the buffer size limitation. Furthermore, the flow amount variables  $f_{m,n}^{b,k}$  and  $\overline{f}_{m,n}^{b,k}$  should satisfy

$$\sum_{n\in\Gamma_m}\sum_{b\in\mathcal{B}_m\cap\mathcal{B}_n}\sum_{k=1}^{K}\overline{f}_{m,n}^{b,k} = a_m, \ \forall m\in\mathcal{R},$$
(31)

$$f_{m,n}^{b,k} \le r_{m,n} e_{m,n} \Delta, \tag{32}$$

$$\overline{f}_{m,n}^{b,k} \le f_{m,n}^{b,k}, \ \overline{f}_{m,n}^{b,k} \le e_{m,n} \Big( k\Delta - \left( \tilde{t}_m a_m + t^{\text{cast}} \right) \Big)^+, \ (33)$$

$$\forall m \in \mathcal{R}, n \in \Gamma_m, b \in \mathcal{B}_m \cap \mathcal{B}_n, k \in \{1, ..., K\},\$$

where (31) ensures that the local aggregated model is transmitted out if this  $PoC^2$  is selected, i.e.  $a_m = 1$ . (32) indicates that the data traffic can be transmitted over link (m, n) only if routing decision  $r_{m,n} = 1$  is made. In (33),  $\overline{f}_{m,n}^{b,k}$  is upper bounded by  $f_{m,n}^{b,k}$  because it is a portion of  $f_{m,n}^{b,k}$ . (33) also ensures that resource tuple ((m, n), b, k) can carry  $\overline{f}_{m,n}^{b,k}$  only after  $PoC^2 m$  aggregates the models from set  $S_m$  of clients, which is analogous to (14). In Problem **P2**, we replace (8) and (25)-(28) with (29)-(33) for  $m \in \mathcal{R}$ , yielding a new problem. While (33) is non-convex, we can linearize it in the same way as we linearize (14), which hence is omitted. Finally, we can employ the enhanced coarse-grained fixing procedure (in Section V-B) to solve the MILP.

TABLE II: Key experimental parameters

D	\$7.1	
Parameters	Values	
Number of $PoC^2$ s $ \mathcal{R} $	16	
Number of channels $ \mathcal{B}_m $	4 or 6	
$PoC^2$ 's transmit power p (dBm)	28	
GBS's downlink transmit power $P$ (dBm)	46	
Transmission range (meters) $R$	350	
Interference range (meters) $R'$	500	
Channel bandwidth W (MHz)	10	
Downlink multicast bandwidth (MHz)	50	
Client's one-epoch update time (seconds)	[1, 2]	
Epoch number	5	
Delay for $PoC^2$ m to aggregate	[0.05.0.2]	
two models $c_m$ (seconds)	[0.05, 0.2]	
The deadline for each	(0)	
training round $D$ (seconds)	60	
The length of control interval $\Delta$ (seconds)	15	
Number of control intervals K	4	
Path loss exponent $\alpha$	4	
Noise power spectral density $N_0$ (W/Hz)	$10^{-16}$	
Antenna-related parameter $\eta$	2.5	

#### VII. PERFORMANCE EVALUATION

In this section, we evaluate the effectiveness of our solution approach and the learning performance of the proposed aggregation scheme.

### A. Simulation Setup

We consider a  $1000 \times 1000m^2$  wireless mesh network, consisting of one GBS at the center and  $16 PoC^2$ s deployed nearby. We assume each  $PoC^2$  provides access services to 10 clients, among which only 3 clients are active at each training round due to sporadic traffic. The transmission and interference ranges for  $PoC^2$ s are 350m and 500m, respectively. We set deadline D = 1 minute for a training round, which is composed of K = 4 control intervals, each lasting 15 seconds.

We adopt two widely used datasets, CIFAR-10 and Fashion MNIST, to evaluate the learning performance. CIFAR contains color images of 10 classes of objects, such as dog, cat, and automobile, whereas Fashion MNIST contains grayscale images of fashion products, such as T-shirt, bag, and dress. These two datasets are good representations of object recognition tasks for many applications, including autonomous driving, smart cameras, e-commerce, etc. CIFAR-10 has 50000 training images and 10000 test images, and Fashion MNIST has 60000 training images and 10000 test images. The training data samples are evenly distributed to 160 clients. We consider both IID settings and non-IID settings. In the IID setting, the data samples are shuffled and evenly partitioned into the clients. In the non-IID setting, each client's data is randomly drawn from 2 classes of samples.

For both datasets, we implement a convolutional neural network (CNN), which consists of convolutional layers with kernel size  $3 \times 3$  and channel number (32, 32, 64, 64, 128, 128). Each convolutional layer is activated by ReLU, and every two

of them is followed by  $2 \times 2$  max pooling. These convolutional layers are followed by three fully connected layers (382 and 192 units with ReLU activation and the last one with 10 units with softmax activation) [16]. The model contains 1.14 millions parameters, and is 4.375 Megabytes in 32-bit float. Each client trains with mini-batch size 32, learning rate 0.01, and momentum 0.5. Notice that higher test accuracy can often be achieved by larger models. Nevertheless, since our goal in this section is to demonstrate the effectiveness of our innetwork aggregation method rather than achieving the best accuracy, such a small-sized model is sufficient for our need. Besides, we set epoch number to 5, i.e., each client performing 5 local updates before uploading. We assume that each client's one-epoch update time is uniformly distributed within [1, 2] seconds, and each client's upload data rate is uniformly distributed within [10, 20] Mbps. The  $PoC^2$  update time  $\tilde{t}_m$ is set to the maximum value among the summations of local update and upload times for the active clients with  $PoC^2 m$ , plus the model aggregation time at  $PoC^2$  m. The aggregation delay at  $PoC^2$ s for one-time model summation, i.e.,  $c_m$ , is drawn from [0.05, 0.1] seconds. Since a macro base station is typically endowed with significantly powerful computing resource, the delay  $c_q$  and  $\overline{c}$  in (17) at GBS are ignored. Given that our laptop takes about 1 second to perform one-epoch training on a client's dataset, and 0.08 seconds to sum up two models, the above parameters are realistic. The following simulation results are averaged from 5 trials with different network topologies. For readers' convenience, we summarize the important experimental parameters in Table II.

We will compare the following strategies.

- In-Network Aggregation Scheme: each *PoC*<sup>2</sup> aggregates all the received models before sending to the next hop, corresponding to the solution to Problem P1.
- Traditional Multi-hop Relaying Scheme: each  $PoC^2$  only aggregates the models from local clients. For the models from other  $PoC^2$ s, it directly relays them to the next hop without aggregation. This scheme corresponds to the solution to the extended problem in Section VI.
- Direct2GBS Scheme: After aggregating the models from local clients, each  $PoC^2$  directly uploads its aggregated model to GBS via one-hop communications. This is a special case of Problem P1 where the transmission set of each  $PoC^2$  only contains GBS. To fully reap the benefits of single-hop communications, we do not consider the limits of transmission range and interference range as in the multi-hop modeling, implying that all  $PoC^2$ s are allowed to directly communicate with GBS (even though the received SNR can be very low due to long distance).

## B. Algorithm Evaluation

Table III compares the proposed coarse-grained fixing procedure with the optimal benchmark. To optimally solve Problem **P2** with a tolerable time, we consider a small-scale problem with 10  $PoC^2$ s and only one channel of 50MHz shared by  $PoC^2$ s. For the enhanced coarse-grained fixing procedure, we set the scale factor { $\beta_1 = 1, \beta_2 = 0.8, \beta_3 = 0.5$ } and threshold  $\theta = 1$ . Since the weighting factors  $w_m$  are the same TABLE III: The number of aggregated models achieved by different strategies versus the number of control intervals K.

K	3	4	5	6	7
Optimal	9.0	15.0	21.0	27.0	30.0
Enhanced coarse-grained fixing	8.4	12.0	16.8	21.6	25.2
Basic coarse-grained fixing	4.8	8.4	13.8	16.8	21.0

TABLE IV: The running time (in seconds) for different strategies versus the number of  $PoC^2s |\mathcal{R}|$ .

<i>R</i>   Strategy	4	8	12	16	20
Enhanced coarse-grained fixing	0.58	1.82	5.40	11.35	30.09
Basic coarse-grained fixing	0.19	0.61	1.80	3.78	10.03

in our parameter settings, the objective of **P2** reduces to maximizing the number of aggregated models. As shown in Table III, the enhanced coarse-grained fixing procedure achieves a reasonable solution to Problem **P2** compared with the optimal benchmark (with about 17.6% performance degradation in average). Besides, due to the multiple trials, the enhanced procedure outperforms the coarse-grained fixing procedure. In fact, the enhanced procedure can be further improved by adding more trials with different scaling factor  $\beta_i$  at the cost of increasing computation overhead.

Note that we have chosen the number of aggregated models as the performance metric. By now, we just assume that more aggregated models generally lead to better training performance, as pointed out in [1], [16], [29]–[31]. This relationship will be studied and confirmed later.

Table IV examines the running time of our proposed schemes versus the number of  $PoC^2$ s, which is conducted via MATLAB on a laptop with 2.60GHz Intel(R) Core(TM) i7-9750H CPU and 16 GB RAM. The running time for both enhanced and basic procedures increases with the the number of  $PoC^2$ s. Depending on the network scale, the running time taken by the basic coarse-grained fixing procedures ranges from 0.19 second to 10.03 seconds, and the time taken by the enhanced procedure is two times longer than the basis one because it solves the problem three times with different scale factors  $\beta_i$ . Note that the number of  $PoC^2$ s (e.g., small base stations) within one macro cell is typically not large in practice. Besides, for a stationary wireless backhaul network where channel gains vary slowly, GBS can collect the channel state information in advance and solve the optimization problem before one training round starts. These imply that our proposed schemes have reasonable running time for practical implementations.

Strategy	The average number of aggregated models per round	Test accuracy at		Time (in minutes) taken to		
		the final dea	adline	achieve a target accuracy		
		CIFAR-10	Fashion	CIFAR-10	Fashion	
			MNIST	@72%	MNIST@90%	
In-network	25.2	77 51%	91 66%	114	115	
aggregation	23.2	11.51%	1.00%	117	115	
Traditional	15.0	72 420%	00 75%	291	146	
Multi-hop relaying	13.0	12.42%	90.75%	201	140	
Direct2GBS	11.4	72.09%	90.47%	399	162	

TABLE V: The training performance for CIFAR-10 and Fashion MNIST with B = 4 channels under IID settings.

## C. Training Performance

Table V shows the test accuracy for the CIFAR-10 and Fashion MNIST at the final deadline (400 minutes) with B = 4 channels under IID settings. As shown in the table, the average number of aggregated models at GBS per round for the proposed in-network aggregation scheme is 25.2, which is 68% more than the traditional multi-hop relaying scheme and 121% more than the Direct2GBS scheme. The Direct2GBS produces the worst performance because the direct model transmissions to GBS suffer from severe path loss resulting from long communication distance. Benefiting from both multi-hop relaying and in-network aggregation, the proposed scheme aggregates the largest number of models and therefore achieves the best test accuracy. For instance, the proposed scheme achieves 77.51% at the final deadline under the CIFAR-10 dataset, which is 5.09% more than the multihop relaying scheme and 5.42% more than the Direct2GBS scheme.

Table V also provides the time required for achieving a target accuracy, where CIFAR-10@72% and Fashion M-NIST@91% indicate the time required for achieving 72% and 91% test accuracy under CIFAR-10 and Fashion MNIST datasets, respectively. It is shown that the proposed in-network aggregation scheme significantly reduces the time taken to achieve a certain accuracy level. For example, the proposed scheme only takes 114 minutes to achieve 72% test accuracy under the CIFAR-10 dataset, whereas other two benchmarks take 281 minutes and 399 minutes to achieve the same accuracy level, respectively.

Fig. 3-4 show the test accuracy curves under CIFAR-10 with B = 4 and B = 6, respectively. In the figures, "Selecting All" assumes that all the active clients' models are aggregated at GBS in each round, which can be regarded as the performance "upper bound". For these figures, it is found that the in-network aggregation scheme outperforms other two benchmark strategies, either under IID or non-IID setting. Moreover, it is not surprising to observe that B = 6 leads to higher test accuracy than B = 4 for the three schemes under both IID and non-IID settings, because more models can be delivered to GBS under more spectrum resource. Furthermore, it is shown that the in-network aggregation scheme brings more significant improvement than other two benchmarks under the case of B = 4 than the case of B = 6. For example, the gap between the in-network aggregation and the traditional multi-hop relaying scheme at the final deadline is 5.09% with



(b) IID settings with B = 6 channels.

Fig. 3: Test accuracy for the CIFAR-10 dataset under IID settings.

B = 4 while being 3.34% with B = 6 under IID settings, implying that the proposed scheme is more beneficial under limited communication resource due to the reduction in data traffic.

## VIII. CONCLUSION

In this paper, we have proposed an FL framework for multihop wireless networks comprising of a mesh of interconnected  $PoC^2$ , where each intermediate  $PoC^2$  performs in-network model aggregation before forwarding the data to the next hop. By considering the heterogeneous communication and computing resources in the wireless mesh network, we have designed a joint routing and spectrum allocation scheme to accelerate the training process. While the formulated problem is



Fig. 4: Test accuracy for the CIFAR-10 dataset under non-IID settings.

a mixed-integer nonlinear programming, we have transformed it into a mixed-integer linear programming, and developed a coarse-grained fixing procedure to find the suboptimal solution efficiently. We have also generalized our problem formulation to the case where some  $PoC^2$ s are not equipped with edge computing capabilities and unable to perform model aggregation. The simulation results have demonstrated the evident advantage of the in-network aggregation scheme over the benchmarks, due to the fact that it can aggregate more models under the limited communication resources.

## APPENDIX A Proof of Theorem1

**Proof:** It is known that finding a maximum independent set in a graph is NP-hard. To prove the theorem, our basic idea is to consider a special case of Problem **P1** such that solving Problem **P1** is equivalent to finding a maximum independent set of a graph. Specifically, we construct a two-tier wireless network where a number of tier-1  $PoC^2$ s directly connect with GBS, and a number of tier-2  $PoC^2$ s connect with the tier-1  $PoC^2$ s. There is no link between the same tier of  $PoC^2$ s. Every  $PoC^2$  has one model to transmit. We assume the number of time interval K = 2, aggregation delay  $c_m = 0$ ,  $\tilde{t}_m^{cast} = 0$ , and weighting factor  $w_m = 1$  for all  $PoC^2$ s. We set  $PoC^2$  update time  $\tilde{t}_m = 0$  for the tier-2  $PoC^2$ s should wait

until the second interval to conduct transmissions. We also set  $e_{m,n}^1 = \frac{1}{\Delta}$  for every link (m, n) such that any resource block can deliver one model within an interval. All  $PoC^2$ s share a common channel, and each tier-1  $PoC^2$  has an additional dedicated channel to communicate with GBS. GBS receives data from tier-1  $PoC^2$ s only through these dedicated channels.

We want to make sure that, under the optimal strategy, every tier-1  $PoC^2$  will transmit during the second interval, such that any model transmitted from a tier-2  $PoC^2$  to any tier-1  $PoC^2$ in the first interval will also be successfully transferred to GBS. This is exactly the case in the constructed network, since each tier-1  $PoC^2$  has a dedicated channel. We define a set of effective resource tuples, including the resource tuples from tier-2 to tier-1  $PoC^2$ s in the first interval, and the resource tuples from tier-1  $PoC^2$ s to GBS in the second interval. It is not hard to see that the optimal objective (the maximum number of aggregated models) of Problem P1 is exactly equal to the number of effective resource tuples that are allocated. We construct a conflict graph G, where the vertices are the effective resource tuples, and the edge between two vertices exists if there is a conflict between them according to (18)-(21). In this way, the optimal objective of Problem P1 is achieved if and only if a maximum independent set of the conflict graph G is found. Therefore, Problem **P1** is NP-hard.

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